

36.1

$k = \text{soil characteristic (when unknown use the following)} = 0.3$

$$w = \text{soil density} = 100 \frac{\text{lb}}{\text{ft}^3}$$

$$h_c = \text{height of wall} = 13\text{ft}$$

$$P_e = \text{max lateral fluid pressure} = kwh_c = (0.3) \left(100 \frac{\text{lb}}{\text{ft}^3} \right) (13\text{ft}) = 390 \frac{\text{lb}}{\text{ft}^2}$$

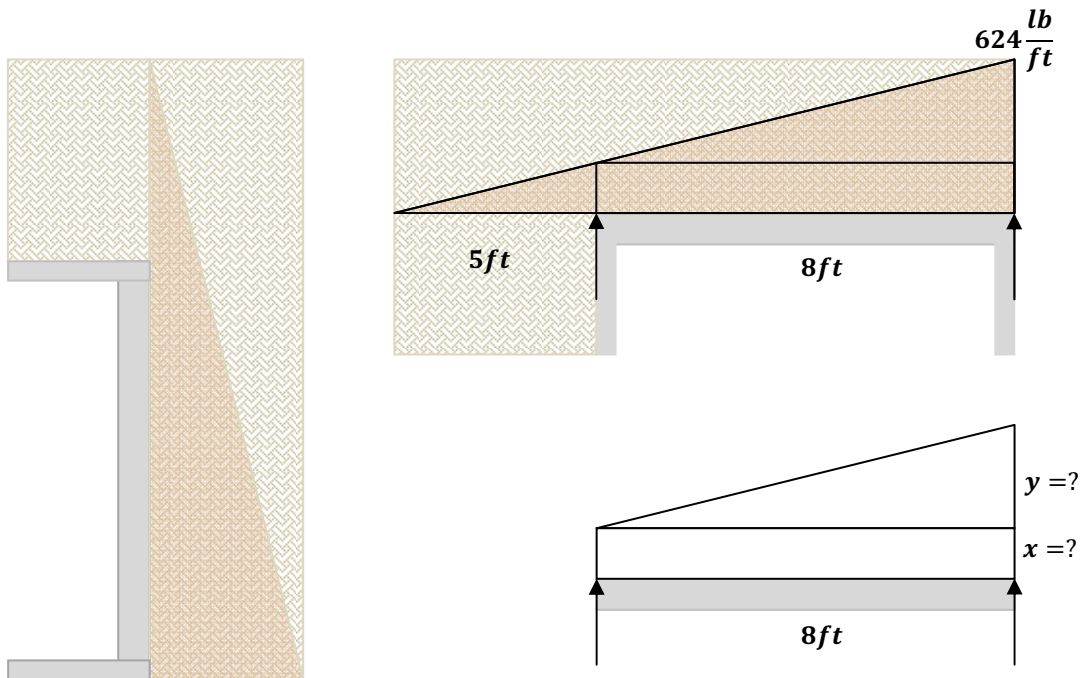
Furthermore, to simplify the problem, we will consider a 1ft wide section of the wall.

See concrete wall diagram.

This will simplify our units to $390 \frac{\text{lb}}{\text{ft}}$. However this value must still be factored for LRFD.

$$1.6 \left(390 \frac{\text{lb}}{\text{ft}} \right) = 624 \frac{\text{lb}}{\text{ft}}$$

The load and span, shear and moment diagram can be visualized as a beam.



Use similar triangles to find the pressure distribution value at the second end of the simplified diagram.

$$\frac{(13\text{ft})}{624 \frac{\text{lb}}{\text{ft}}} = \frac{8\text{ft}}{y}$$

$$13\text{ft}(y) = 8\text{ft} \left(624 \frac{\text{lb}}{\text{ft}} \right)$$

$$y = \frac{8\text{ft} \left(624 \frac{\text{lb}}{\text{ft}} \right)}{13\text{ft}} = 384 \frac{\text{lb}}{\text{ft}}$$

$$x = 624 \frac{\text{lb}}{\text{ft}} - y = \left(624 \frac{\text{lb}}{\text{ft}} \right) - \left(384 \frac{\text{lb}}{\text{ft}} \right) = 240 \frac{\text{lb}}{\text{ft}}$$

To simplify the problem, analyze the loading as a rectangle and a square.

Find the total load W:

Area of a Triangle = $\frac{1}{2}(\text{base})\text{height}$



$$W_T = \frac{1}{2}(8ft)384 \frac{lb}{ft} = 1536lb$$

Area of a rectangle = $(\text{base})\text{height}$



$$W_S = (8ft)240 \frac{lb}{ft} = 1920lb$$

Find Shear Max V:



Max shear of a triangular load = $\frac{2}{3}W_T$

$$V_T = \frac{2}{3}(1536lb) = 1024 lb$$



Max shear of a rectangular load = $\frac{1}{2}W_S$

$$V_S = \frac{1}{2}(1920lb) = 960 lb$$

Find the Total Shear



$$V_u = V_T + V_S = 1024 lb ft + 960 lb ft = \mathbf{1984lb}$$

Find Max Moment M:



Max moment of a rectangular load = $0.1283W_T L$

$$M_T = \frac{2}{3}(1536lb) = 1576 lb ft$$



Max moment of a rectangular load = $\frac{W_S L}{8}$

$$M_S = \frac{1}{2}(1920lb) = 1920 lb ft$$

Find the Total Moment



$$M_u = M_T + M_S = 1576lb ft + 1920 lb ft = 3496lbft \left(\frac{12in}{1ft}\right) = 41952bin = \mathbf{42k in}$$

To determine if a 8in wall will be adequate find the following:

1. Find the depth required for the maximum moment

$$d_m = \sqrt{\frac{M_u}{\Phi R b}}$$

2. Find the depth required for the maximum shear

$$V_{crit} = V_u - (P_e)d_v$$

$$f'_v = \frac{V_{crit}}{A}$$

3. Find the code required depth

4in or L/25

Proceed with the following conditions:

$$f'_c = 3000\text{psi}$$

$$F_y = 60000\text{psi}$$

$$\rho_{rec} = 0.0080\text{psi (from table A.4)}$$

$$R = \text{required reinforcement} = 434.7\text{psi (from table A.7)}$$

$$b = 12\text{in (one foot section of the wall)}$$

$$M_u = 42\text{k in}$$

$$\phi = 0.9$$

$$P_e(\text{at } 13\text{ft and factored}) = \text{max lateral fluid pressure} = kwh_c = 624 \frac{\text{lb}}{\text{ft}}$$

$$f'_v = 82.2\text{psi (table 31.1)}$$

$$V_u = 1984\text{lb}$$

Find the depth required for the maximum moment

$$d_m = \sqrt{\frac{M_u}{\Phi R b}} = \sqrt{\frac{42\text{k in}}{(0.9)(434.7)(12\text{in})}} = 2.99\text{in}$$

Find the depth required for the maximum shear

$$V_{crit} = V_u - (P_e)d_v$$

$$f'_v = \frac{V_{crit}}{A}$$

Combine the equations:

$$f'_v = \frac{V_u - (P_e)d_v}{b(d_v)}$$

Rearrange:

$$f'_v(b)(d_v) = V_u - (P_e)d_v$$

$$f'_v(b)(d_v) + (P_e)(d_v) = V_u$$

Factor:

$$d_v(f'_v b + P_e) = V_u$$

$$d_v = \frac{V_u}{(f'_v b + P_e)} = \frac{1984lb}{\left(82.2psi(12in) + 624\frac{lb}{ft}\left(\frac{1ft}{12in}\right)\right)} = \frac{1984lb}{1038.4\frac{lb}{in}} = \mathbf{1.91in}$$

Find the code required depth

Code requires 4in or L/25:

$$\frac{L}{25} = \frac{8ft\left(\frac{12in}{ft}\right)}{25} = 3.84in$$

Since $3.84in < 4in$

$$\mathbf{d_c = 4in}$$

Summarize conclusions:

$$\mathbf{d_m = 2.99in}$$

$$\mathbf{d_v = 1.91in}$$

$$\mathbf{d_c = 4in}$$

Since they are all less than 8in the wall depth will be sufficient.

Size steel for the 8in wall depth:

$$b = 12in$$

$$d = 8in - 2in = 6in \text{ (2in is the concrete cover over the steel)}$$

$$d_m = \sqrt{\frac{M_u}{\Phi R b}}$$

Rearrange to find the actual required reinforcement value R:

$$R = \frac{M_u}{\Phi d^2 b} = \frac{42k \text{ in}}{0.9(6in)^2(12in)} = 0.108ksi = 108psi$$

Use table A.8 to find R (however, the value is off the chart so use the minimum value of

$$\rho_g \text{ (aka } \rho_{min}) = 0.033$$

$$A_s = \rho_{min} A_c = (0.033)12in(6in) = 0.24in^2 \text{ per one foot of spacing}$$

$$\text{Try \#4 bar: Area} = 0.2in^2$$

$$\frac{0.24in^2}{12in} = \frac{0.2in^2}{\text{spacing}}$$

Spacing = 10in with #4 bar